



MOCK TEST JEE -2020
TEST-02 ANSWER KEY

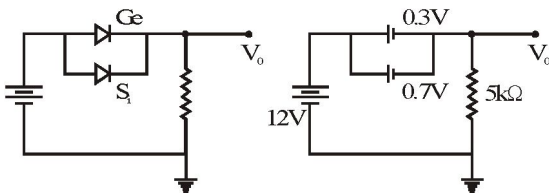
Test Date :03-01-2020

[PHYSICS]

1.

Ans. (2)

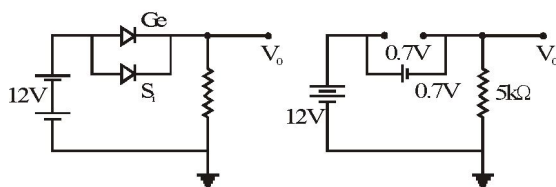
initially



As resistances of diodes are negligible w.r.t. load resistance

$$V_0 = 12 - 0.3 = 11.7 \text{ Volt}$$

Finally



$$V_0 = 12 - 0.7 = 11.3 \text{ Volt}$$

2.

Ans. (1)

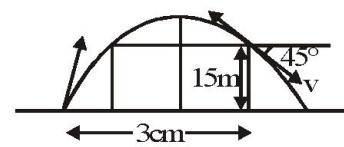
In FM, modulation index

$$= \frac{\text{frequency deviation}}{\text{modulation frequency}}$$

$$= \frac{50 \times 10^3}{7 \times 10^3} = 7.143$$

3.

Ans. (4)



$$y = x \tan \theta - \frac{gx^2(1 + \tan^2 \theta)}{2u^2}$$

$$x^2 = \frac{30 \times 30 \times 10}{45 \times 2}$$

$$x^2 = 100$$

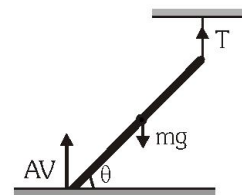
$$V^2 = x^2 + 2 \times 10 \times 15$$

$$V^2 = 500$$

$$\Rightarrow V = \sqrt{500} \text{ m/s}$$

4.

Ans. (1)



$$Mg = N + T \quad \dots(1)$$

Torque about com will be zero.

$$\therefore N \times \frac{l}{2} \cos \theta = T \times \frac{l}{2} \cos \theta = 0$$

$$N = T$$

$$\therefore T = \frac{mg}{2}$$

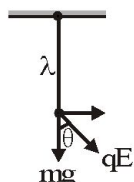
5.

Ans. (2)

Pendulum will perform oscillatory motion with extreme positions along gravitational force and electrostatic forces.

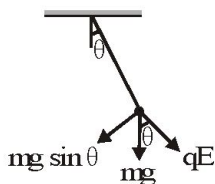
(1) When pendulum is vertical

$$\text{torque about line} = qE \sin \theta \times \ell$$



(2) When pendulum is along electric field

$$\text{torque about image} = mg \sin \theta \times \ell$$



$$\therefore E = \frac{mg}{q}$$

6.

Ans. (1)

$$T^2 = 2\pi \sqrt{\frac{\ell}{g_{\text{eff}}}}$$

ℓ = length of threads

$$T^1 = \frac{T}{\sqrt{2}}$$

where $T = 2\pi \sqrt{\frac{\ell}{g}}$

$$g_{\text{eff}} = 2g = (g + a)$$

$$\therefore \text{net downwards force} = 2mg = mg + iBL$$

$$\therefore i = \frac{mg}{BL}$$

7.

Ans. (1)

$$n = \frac{180}{18} = 10 \text{ moles}$$

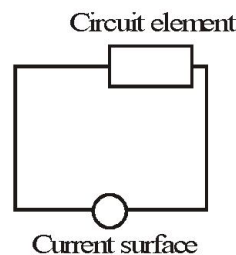
$$PV = nRT$$

$$P \times 0.1 = 10 \times 8.314 \times 1000$$

$$P = 8.314 \times 10^5 \text{ Pa}$$

8.

Ans. (4)



$$\frac{dV}{dt} = \frac{8-2}{3} = 2$$

Potential rises with time across capacitor $Q = CV$

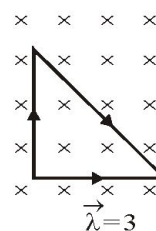
$$\frac{dQ}{dt} = i = C \frac{dV}{dt}$$

$$1 = C \times 2$$

$$\Rightarrow C = 0.5 \text{ F}$$

9.

Ans. (2)



Force due to magnetic field

$$= i(\vec{\ell} \times \vec{B}) = 2 \times [0.03\hat{i} \times 2(-\hat{k})] = (0.12\hat{j})\text{N}$$

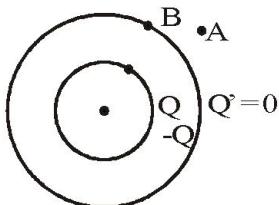
$$\therefore \text{Acceleration} = \frac{F}{m}$$

$$= \frac{0.12}{10 \times 10^{-3}} = (12\text{m/s}^2)\hat{j}$$

10.

Ans. (4)

There will be no change on outer surface of outer sphere.



$$\therefore V_A = V_B = 0$$

$$V_0 = \frac{kQ}{r_a} - \frac{kQ}{r_b} = \frac{Q}{4\pi\epsilon_0} \left[\frac{1}{r_a} - \frac{1}{r_b} \right]$$

But $V_C \neq 0$

11.

Ans. (1)

$$A = A_0 e^{-\frac{b}{2m}t}$$

$$A = A_0 e^{-\frac{xt}{2\delta Ld}}$$

12.

Ans. (3)

$$|V| = \left| -\frac{d\phi}{dt} \right| = \oint \vec{E} \cdot d\vec{l}$$

$$\Rightarrow \pi b^2 \frac{B}{\Delta t} = E \times 2\pi a$$

\therefore Force on circular wheel

$$= E \times q = E \times 2\pi a \times \lambda = \frac{\pi b^2 B}{\Delta t} \times \lambda$$

$$\text{Torque about centre} = a \times F = \frac{\pi b^2 B}{\Delta t} \times \lambda a = I_C \alpha$$

$$\therefore I_C \times \frac{\omega}{\Delta t} = \frac{\pi b^2 B \lambda a}{\Delta t}$$

$$\therefore \omega = \frac{\pi b^2 B \lambda a}{I_C} = \frac{\pi b^2 a B \lambda}{2I}$$

13.

Ans. (2)

Since momentum is transferred to mirror so reflected light is of less momentum so it will have more wavelength.

14.

Ans. (4)

$$\lambda = \frac{h}{\sqrt{2mT_A}}$$

$$\Rightarrow T_A = \frac{h^2}{2m\lambda_A^2}$$

$$T_B = T_A - 1.5$$

$$\frac{h}{4 \times 2m\lambda_A^2} = \frac{h}{\lambda_A^2 \times 2m} - 1.5$$

$$\frac{3}{4} \times \frac{h}{2m\lambda_A^2} = 1.5 \text{ eV}$$

$$\Rightarrow T_A = \frac{h}{2m\lambda_A^2} = 2.00 \text{ eV}$$

$$\therefore T_B = T_A - 1.5 = 0.5 \text{ eV}$$

$$\therefore 2 = 4.25 - \phi_A$$

$$0.5 = 4.7 - \phi_B$$

$$\Rightarrow \phi_B = 4.2 \text{ eV}$$

15.

Ans. (3)

By newton's formula $f^2 = x \cdot x'$

$$\therefore |m| = \frac{f+x'}{f+x} = \frac{V}{x}$$

$$= \frac{fx+f^2}{fx+x^2} = \frac{f(f+x)}{x(f+x)}$$

$$|m| = \frac{f}{x}$$

16.

Ans. (4)

Mass of spherical shell of width 'dr' of radius
= dm

$$= \rho_0 \left(1 - \frac{r^2}{R^2} \right) \cdot 4\pi r^2 \cdot dr$$

$$\therefore m = \int_0^R dm$$

$$= \frac{\rho_0}{R^2} \int_0^R (R^2 - r^2) 4\pi r^2 dr$$

$$= \frac{\rho_0 \times 4\pi}{R^2} \left[R^2 \int_0^R r^2 dr - \int_0^R r^4 dr \right]$$

$$\therefore m = \frac{\rho_0 \times 4\pi}{R^2} \left[\frac{R^5}{3} - \frac{R^5}{5} \right]$$

$$m = \frac{\rho_0 \times 8\pi R^3}{15}$$

\therefore Gravitational force on unit mass of $r > R$

$$\therefore F = \frac{GM \times 1}{r^2} = \frac{G \times 8\pi \rho_0 R^3}{15r^2}$$

17. **Ans. (2)**

$$V = \frac{\pi d^2}{4} \times h$$

vernier scale reading = (6 ± 0.01) cm

ruler scale reading = (10 ± 1) cm

$$\therefore \left(\frac{\Delta V}{V} \right) = \left(2 \frac{\Delta d}{d} + \frac{\Delta h}{h} \right)$$

$$\therefore \frac{\Delta V}{V} \% = \left(\frac{2 \times 0.1}{6} + \frac{1}{10} \right) \times 100\%$$

$$= 0.1 + 0.033$$

$$= 0.133 \times 10\%$$

$$= 13.3 \%$$

18.

Ans. (1)

Length of micro scope tube = $v_0 + u_e = \ell$ on
increasing length $u_e \uparrow$

$$m = \frac{v_0}{u_0} \times \frac{v}{u_e}$$

$$\therefore u_e \uparrow \Rightarrow m \downarrow$$

19.

Ans. (4)

$$\ell = n \frac{\lambda}{2} \Rightarrow \lambda = \frac{2\lambda}{n}$$

$$f = \frac{nV}{2\ell}$$

$$400 = \frac{n \times 350}{2\ell}$$

$$\ell = \frac{n \times 350}{800} = \frac{7}{16}n$$

$$n = 1, 2, 3, \dots$$

20.

Ans. (1)

$$V = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{10}{0.1}} = 10 \text{ m/s}$$

$$y = 2 \sin(20t - 2x)$$

$$\frac{\partial y}{\partial t} = v_p = 0.02 \cos(t - 2x)$$

Energy density

$$= \frac{I}{V} \times \text{Area} = \frac{\partial \times A^2 \omega^2 \cos^2(\omega t - kx) \times \text{Area} \times v}{v}$$

At near position,

$$\text{Energy density} = \mu \times A^2 \omega^2$$

$$= 0.1 \times 4 \times 10^{-4} \times 400$$

$$= 1.6 \times 10^{-2} \text{ J/m}$$

21.

$$f = \frac{1}{2\ell} \sqrt{\frac{T}{\mu}}$$

$$f = \frac{f}{2} = \frac{1}{2\ell} \sqrt{\frac{T'}{\mu}}$$

$$\therefore T' = \frac{T}{4} = \frac{12 \times g}{4}$$

$$\therefore \text{mass} = 3 \text{ kg}$$

$$\therefore \text{removed mass} = 9 \text{ kg}$$

22. **3**23. **2**24. **4**25. **3**

[CHEMISTRY]

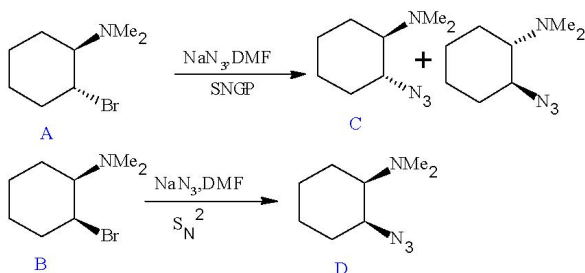
26.

Ans. (2)

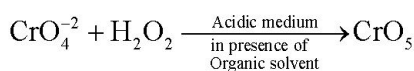
$$\lambda_{(\text{NaBr})} = \lambda_{\text{Na}^+} \times X_{\text{Br}^-} = 12 \times 10^{-3}$$

$$\lambda = \frac{K}{1000 \times M} \Rightarrow K = 12 \times 10^{-3} \times 10^3 \times 0.1 = 1.2$$

27.

Ans. (2)

28.

Ans. (1)

29.

Ans. (1)

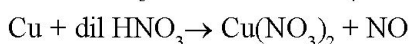
$$n = \frac{PV}{ZRT} = \frac{81.06 \times 10^6 \times V_1}{1.95 \times R \times 223} \quad (\text{i})$$

$$n = \frac{20.265 \times 10^6 \times V_2}{1.1 \times R \times 373} \quad (\text{ii})$$

$$\frac{20.265 \times 10^6 \times V_2}{1.1 \times R \times 373} = \frac{21.06 \times 10^6 \times 10\text{m}^3}{1.95 \times R \times 223}$$

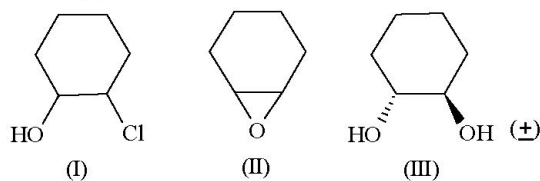
$$V_2 = 3.77$$

30.

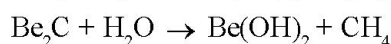
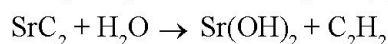
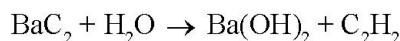
Ans. (2)

Au, Cu : transition metals. NO : paramagnetic colourless gas.

31.

Ans. (4)

32.

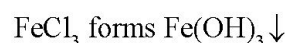
Ans. (3)

33.

Ans. (3)

Gold number is 0.06 so 0.06mg will be required for 10 ml, so for 100 ml 0.6 mg will be required.

34.

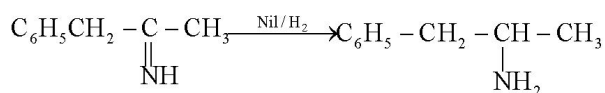
Ans. (1)

35.

Ans. (2)

Facts

36.

Ans. (2)

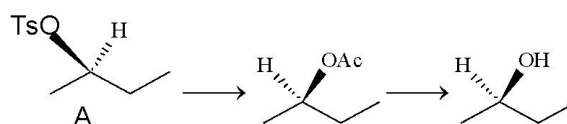
Addition-elimination

37.

Ans. (4)

H_2O_2 produces electrolysis followed by hydrolysis.

38.

Ans. (2)

39. (4)

40. (1)

41.

Ans. (1)

0.06 ppm, so in 10^6 ml water = 0.06 gm SO_2

$$[\text{SO}_2] = \frac{0.06}{64 \times 10^3} = \frac{6}{64} \times 10^{-5}$$

$$[\text{H}^+] = \frac{12}{64} \times 10^{-5}, \text{ So pH} = 5 - (\log 12 - \log 64) = 5.7$$

42.

Ans. (3)

Mozingo reduction.

43.

Ans. (3)

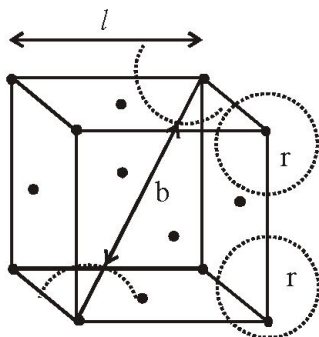
$d_{x^2-y^2}$: e^- density is present along x & y axis.

d_{z^2} : e^- density is in xy plane also.

44.

Ans. (1)

given $\frac{a}{b} = \frac{1}{2}$



then length (a) = $1 - 2r$

then length (b) = $1\sqrt{3} - 2r$

$$\frac{1 - 2r}{1\sqrt{3} - 2r} = \frac{1}{2}$$

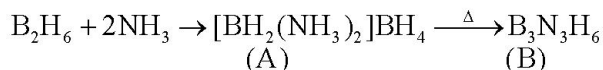
$$21 - 4r = 1\sqrt{3} - 2r$$

$$21 - 1\sqrt{3} = 2r$$

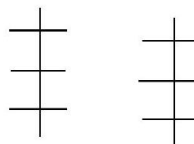
$$\frac{r}{1} = \left(\frac{2 - \sqrt{3}}{2} \right) = 0.134$$

45.

Ans. (4)



46. 2



47.

Meq of $\text{Mg}^{+2} = \text{Meq of washing soda}$

$$\frac{W}{E} \times 1000 = \text{Mg}^{+2}; \text{EW} = \frac{24}{2} = 12$$

$$\frac{12 \times 10^{-3}}{12} \times 1000 = 1.$$

48.

$$E = hv = h \frac{c}{\lambda} \text{ i.e. } E \propto \frac{1}{\lambda}$$

$$\frac{E_1}{E_2} = \frac{\lambda_2}{\lambda_1} = \frac{4000}{2000} = 2.$$

49.

$$\frac{1}{\lambda} = R_H \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

$$= \frac{1}{\lambda} = R_H \left[\frac{1}{3^2} - \frac{1}{n_2^2} \right] = n_2 = 3 \text{ for Paschen series.}$$

50.

BeF_3^- does not show sp^3 -hybridization because this compound is not formed.

[MATHEMATICS]

51. **Ans. (2)**

$$x - \frac{x^3}{6} < \sin x < x \quad \forall x > 0$$

$$\Rightarrow f\left(x - \frac{x^3}{6}\right) > f(\sin x) > f(x)$$

$$\Rightarrow \frac{f\left(x - \frac{x^3}{6}\right)}{f(x)} < \frac{f(\sin x)}{f(x)} < 1$$

$$\Rightarrow \lim_{x \rightarrow \infty} \frac{f\left(x - \frac{x^3}{6}\right)}{f(x)} < \lim_{x \rightarrow \infty} \frac{f(\sin x)}{f(x)} < 1$$

52. **Ans. (1)**

$$f'(x) = (3\sin^2 x + 2\lambda \sin x)\cos x$$

$$= 3 \sin x \cos x \left(\sin x + \frac{2\lambda}{3} \right)$$

$\sin x$ is increasing for $-\frac{\pi}{2} < x < \frac{\pi}{2}$

$$\Rightarrow -1 < -\frac{2\lambda}{3} < 0 \Rightarrow 0 < \lambda < \frac{3}{2}$$

53.

Ans. (4)

$$x^3 - x + \frac{1}{x} - \frac{k}{x^2} = 0$$

$$\Rightarrow x^6 - x^4 + x^2 - kx = 0 \quad \dots (i)$$

and $x^4 - x^2 + 1 - \frac{k}{x} = 0 \quad \dots (ii)$

Adding (i) & (ii)

$$x^6 + 1 = k \left(x + \frac{1}{x} \right) \geq 2 \quad [\because x > 0]$$

$$\Rightarrow \int_0^1 x^6 dx \geq \int_0^1 (2k - 1) dx \Rightarrow \int_0^1 x^6 dx \geq 2k - 1$$

But $\int_0^1 x^6 dx \geq \frac{1}{10}$

$$\therefore 2k - 1 \leq \frac{1}{10} \Rightarrow k \leq \frac{11}{20}$$

54.

Ans. (1)

$$x \in (1, e) \Rightarrow \log x \in (0, 1)$$

$$\log x > (\log x)^2$$

$$\Rightarrow \frac{\log x}{1-x} < \frac{(\log x)^2}{1-x}$$

$$\Rightarrow -\frac{1}{x} < \frac{1}{1-x} < \frac{\log x}{1-x} < \frac{\log^2 x}{1-x}$$

So, $-1 < I_1 < I_2$

55.

Ans. (4)

$$\cos^3 20^\circ - \sin^3 10^\circ - \sin^3 50^\circ$$

$$\cos^3 \theta = 4\cos^3 \theta - 3\cos \theta$$

$$\sin^3 \theta = 3\sin \theta - 4\sin^3 \theta$$

$$\Rightarrow \frac{\cos 60^\circ + 3\cos 20^\circ}{4} - \left(\frac{3\sin 10^\circ - \sin 30^\circ}{4} \right)$$

$$- \left(\frac{3\sin 50^\circ - \sin 150^\circ}{4} \right)$$

$$= \frac{1}{4} [\cos 60^\circ + 3(\cos 20^\circ - \sin 10^\circ - \sin 50^\circ)$$

$$+ \sin 30^\circ + \sin 150^\circ]$$

$$= \frac{1}{4} \left[\frac{3}{2} + 3(\cos 20^\circ - 2\sin 30^\circ \cos 20^\circ) \right]$$

$$= \frac{3}{8} + 0 = \frac{a}{b}$$

$$b - a = 8 - 3 = 5$$

56.

Ans. (2)

$$\sum_{r=1}^5 {}^{20}C_{2r-1} = k \Rightarrow {}^{20}C_1 + {}^{20}C_3 + {}^{20}C_5 + {}^{20}C_7 + {}^{20}C_9$$

$$\Rightarrow {}^{20}C_1 + {}^{20}C_3 + \dots + {}^{20}C_9 = 2^{18}$$

$$k^6 = (2^{18})^6 \Rightarrow 2^{108} = 2^3 [2^{105}]$$

$$= 8 [2^{21 \times 5}] = 8 [32]^{21} = 8 [33 - 1]^{21}$$

$$= 8 [M(11) - 1] = 8M(11) - 8 = 8M(11) - 11 + 3$$

$$= (8M(11) - 11) + 3$$

57.

Ans. (1)

Unit's place at $3^{4n} = 1, 3^{4n+1} = 3, 3^{4n+2} = 9, 3^{4n+3} = 7$

Units place at $7^{4n} = 1, 7^{4n+1} = 7, 7^{4n+2} = 9, 7^{4n+3} = 3$

We have 25 probability each for $4n, 4n + 1, 4n + 2, 4n + 3$

Now, for digit equal to 8 at units place

$$P = \frac{25 \times 25 + 25 \times 25}{100 \times 99} = \frac{1850}{9900} = \frac{37}{198}$$

58.

Ans. (2)

$$S_n = \sum_{r=1}^n \frac{2r+1}{r^2(r+1)^2} = \sum_{r=1}^n \left(\frac{1}{r^2} - \frac{1}{(r+1)^2} \right)$$

$$S_{20} = \left(\frac{1}{1} - \frac{1}{2^2} \right) + \left(\frac{1}{2^2} - \frac{1}{3^2} \right) + \dots + \left(\frac{1}{20^2} - \frac{1}{21^2} \right)$$

$$S_{20} = 1 - \frac{1}{441} = \frac{440}{441}$$

$$\text{So, } \sqrt{n+1} = \sqrt{441} = 21$$

59.

Ans. (3)

$\angle PAD = 39^\circ = \angle DBA$ (Alternate segments are asked)

$$\angle BCD = 103^\circ$$

$$\angle BAD = 77^\circ$$

$$\angle ADB = 180^\circ - 77^\circ - 39^\circ = 64^\circ$$

60.

Ans. (4)

E _ _ E _ _ _

Total 4 possibilities and to arrange NWYRA we can arrange them in $5!$ ways

$$\text{Total} = 5! \times 4 = 480$$

Answer = $480 - 1 = 479$ (as rearrangements are asked)

61.

Ans. (3)

$$D > 0$$

For this maximum value of $k = 6 = 2 \times 3$

$$\text{So, number of divisors} = (1+1)(1+1) = 4$$

$$\text{So, number of proper divisors} = 4 - 2 = 2$$

62.

Ans. (3)

We have, $\log \frac{dy}{dx} = 9x - 6y + 6$

$$\Rightarrow \frac{dy}{dx} = e^{9x+6} \cdot e^{-6y}$$

$$\Rightarrow e^{6y} dy = e^{9x+6} dx$$

$$\text{Integrating, } \frac{e^{6y}}{6} = \frac{e^{9x+6}}{9} + c$$

Putting $x = 0, y = 1$; we get

$$\frac{e^6}{6} = \frac{e^6}{9} + c \Rightarrow c = \frac{e^6}{18}$$

$$\therefore \text{Solution is } \frac{e^{6y}}{6} = \frac{e^{9x+6}}{9} + \frac{e^6}{18}$$

$$3e^{6y} = 2e^{9x+6} + e^6$$

63.

Ans. (1)

If a line makes angle $\theta_1, \theta_2, \theta_3$ with the planes $x=0, y=0, z=0$ then

$$\sin^2 \theta_1 + \sin^2 \theta_2 + \sin^2 \theta_3 = 1$$

Here, $\theta_1 = \theta_2 = \alpha$

$$\therefore 2\sin^2 \alpha + \sin^2 \theta_3 = 1$$

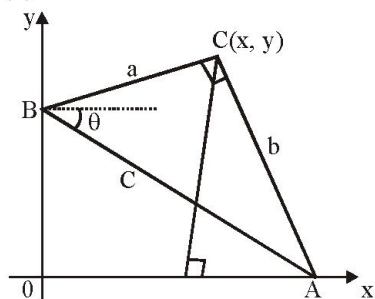
$$1 - 2\sin^2 \alpha = \sin^2 \theta_3 \geq 0$$

$$\cos 2\alpha \geq 0$$

$$\Rightarrow 2\alpha \in \left[0, \frac{\pi}{2} \right] \Rightarrow \alpha \in \left[0, \frac{\pi}{4} \right]$$

64.

Ans. (1)



$$x = a \cos(B - \theta) = a \cos B \cos \theta + a \sin B \sin \theta$$

$$= \frac{a^2}{c} \cos \theta + \frac{ab}{c} \sin \theta = \frac{a}{c} (a \cos \theta + b \sin \theta)$$

$$y = b \sin(\theta + A) = b \sin \theta \cos A + b \cos \theta \sin A$$

$$= \frac{b^2}{c} \sin \theta + \frac{ab}{c} \cos \theta = \frac{b}{c} (b \sin \theta + a \cos \theta)$$

$$\therefore \frac{y}{x} = \frac{b}{a}; \text{ straight line}$$

65.

Ans. (2)

$$\sqrt{3} = \left| (\vec{b} - \vec{a}) \cdot \frac{(\vec{p} \times \vec{q})}{|\vec{p} \times \vec{q}|} \right|$$

$$\Rightarrow \sqrt{3} = |\vec{b} - \vec{a}| \cos 30^\circ \Rightarrow |\vec{b} - \vec{a}| = AB = 2$$

66.

Ans. (2)

$$\text{Clearly, } \vec{r} \cdot \vec{a} = \beta [\vec{a} \cdot \vec{b} \cdot \vec{c}] = \frac{1}{8} \beta$$

$$\vec{r} \cdot \vec{a} = \beta [\vec{a} \cdot \vec{b} \cdot \vec{c}] = \frac{1}{8} \beta$$

$$\vec{r} \cdot \vec{b} = \gamma [\vec{a} \cdot \vec{b} \cdot \vec{c}] = \frac{1}{8} \gamma$$

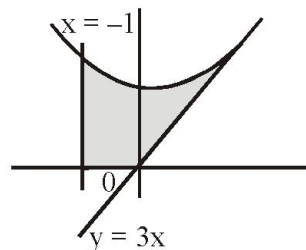
$$\therefore \vec{r} \cdot (\vec{a} + \vec{b} + \vec{c}) = \frac{1}{8} (\alpha + \beta + \gamma)$$

$$\therefore \alpha + \beta + \gamma = 8 \vec{r} \cdot (\vec{a} + \vec{b} + \vec{c})$$

67.

Ans. (2)

Equation of tangent is $y = 3x$



$$A = \int_{-1}^0 (x^2 + x + 1) dx + \int_0^1 (x^2 + x + 1 - 3x) dx = \frac{7}{6}$$

68.

Ans. (1)

$$N = k({}^n C_0 + {}^n C_1 + \dots + {}^n C_n) = k \cdot 2^n$$

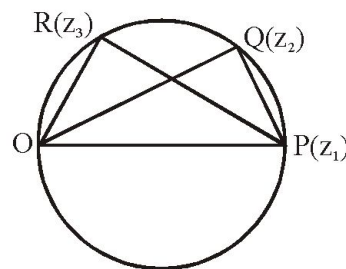
$$\sum f_i x_i = k \cdot n (2)^{n-1}$$

$$\bar{x} = \frac{n \cdot 2^{n-1}}{2^n} = \frac{n}{2}$$

69.

Ans. (1)

In terms of \overline{OP} (z_1), z_2 & z_3 are easily obtainable by rotation about the point O.



Thus, $z_2 = z_1 \cos \theta e^{i\theta}$, $z_3 = z_1 \cos 2\theta e^{i2\theta}$

$$\therefore \frac{z_1 z_3}{z_2^2} = \frac{\cos 2\theta}{\cos^2 \theta}$$

70.

Ans. (2)

$$f(x) \cdot f'(-x) = f(-x) \cdot f'(x)$$

$$f'(x) \cdot f(-x) - f(x)f'(-x) = 0$$

$$\frac{d}{dx}(f(x)f(-x)) = 0$$

$$f(x) \cdot f(-x) = k, \text{ given } (f(0))^2 = k$$

$$\text{Then } f(3) \cdot f(-3) = 9$$

71.

$$\text{Since } f^{-1} \circ g^{-1}(x) = (g \circ f)^{-1}(x)$$

domain of $(g \circ f)^{-1}(x)$ is range of $g \circ f(x)$ which is $[-5, -2]$.

\Rightarrow Number of integers are 4

72.

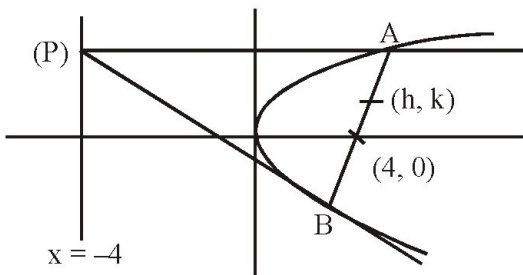
$$AX = \lambda X \Rightarrow (A - \lambda I)X = O$$

$$X \neq O \Rightarrow \begin{vmatrix} 4-\lambda & 6 & 6 \\ 1 & 3-\lambda & 2 \\ -1 & -5 & -2-\lambda \end{vmatrix} = 0$$

$$\Rightarrow (\lambda - 1)(\lambda - 2)^2 = 0$$

$$\Rightarrow \lambda = 1, 2$$

73.



Equation of AB

$$T = S_1$$

$$yk - 8(x + h) = k^2 - 16h$$

this chord passing through $(4, 0)$

$$0 - 8(4 + h) = k^2 - 16h$$

$$y^2 = 8(x - 4)$$

So, focus is $(6, 0)$

74.

Ans. (4)

$$f(x) = 1 - \tan^{2n}x$$

$$f\left(\frac{\pi}{4}\right) = 0$$

$$\text{Now, } \left[\sec\left(0 + \frac{\pi}{4}\right) \right] = [\sqrt{2}] = 1$$

75.

Ans. (3)

$$P_n = \cos\left(\frac{x}{2^1}\right) \cos\left(\frac{x}{2^2}\right) \cos\left(\frac{x}{2^3}\right) \dots \cos\left(\frac{x}{2^n}\right)$$

$$= \frac{\sin 2^n \cdot \left(\frac{x}{2^n}\right)}{2^n \sin\left(\frac{x}{2^n}\right)} = \frac{\sin x}{2^n \sin\left(\frac{x}{2^n}\right)}$$

$$g(x) = \lim_{x \rightarrow \infty} \frac{x \sin x}{(2^n) \sin\left(\frac{x}{2^n}\right)} = \sin x$$

In $[0, 4\pi]$ $\sin x = -1$ has two solutions

